

BJT Small Signal Analysis.

1.

→ They are two types of signal analysis available

- * Small signal Amplifier
- * large signal Amplifier.

parameters of Amplifier.

* parameters are factors, these decide the performance of an amplifier.

- * Input Impedance * Output Impedance
- * Amplification factor *

↳ voltage gain

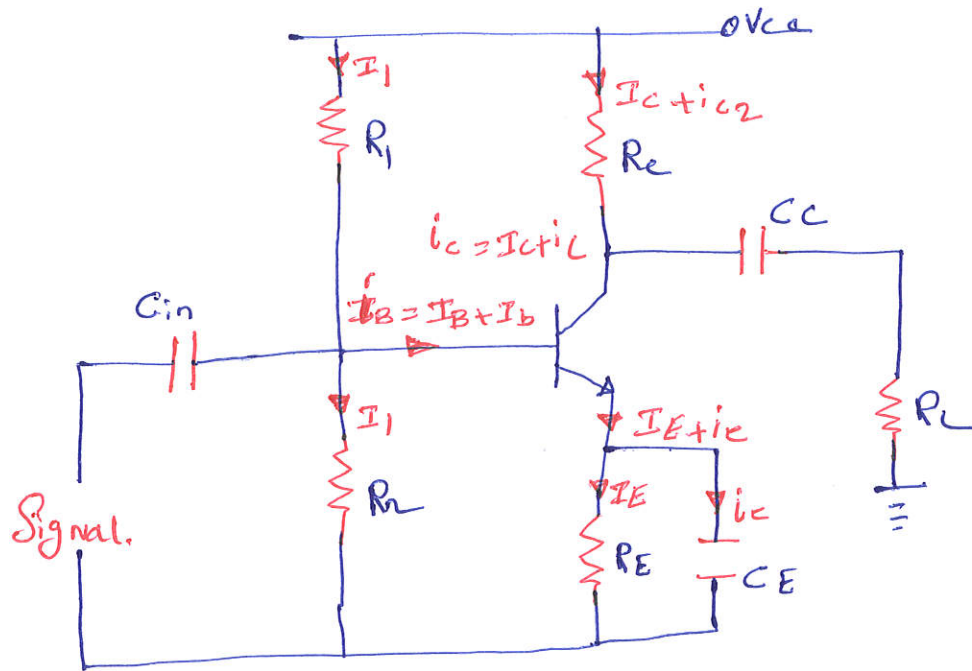
↳ current gain

↳ power gain.

Practical circuit of Transistor Amplifier.

basic components.

- * Biasing ckt
- * Input capacitor C_{in}
- * Emitter bypass capacitor
- * coupling capacitor



i) Biassing circuits.

* The Resistance R_1 , R_2 , & R_E form the biasing and stabilisation circuit.

* The biasing circuit must establish proper operating point.

* otherwise a part of the negative half cycle of the signal may be cut off in the output.

ii) Input capacitance. ($\approx 10\text{ nF}$)

* capacitor used to couple the signal to the base of the transistor.

iii] Emitter bypass capacitor C_E $\approx 100\mu F$

$\rightarrow C_E$ is used to parallel with R_E to provide low Resistance Reactance path to the amplified a.c. signal, if it is not used.

* Amplified a.c. signal flowing through R_E will cause a voltage drop across it. thereby reducing the output voltage.

iv) Coupling capacitor C_C $\approx 10\mu F$

* The coupling capacitor couples one stage of amplification to the next stage. if it is not used.

* The bias conditions of next stage will be drastically changed due to the shunting effect of R_C

In short

C_C isolates d.c. of one stage from next stage. but allows passage of a.c. signal.

Various circuit currents.

i) Base current

$$i_B = I_B + i_b.$$

* when no signal is applied in the base circuit, d.c. base current I_B flows due to biasing circuits.

* when a.c. signal is applied, a.c. base current i_b also flows. $\therefore$

total current $i_B = I_B + i_b$

ii) Collector current

No signal $\Rightarrow I_C$ flows $\rightarrow$ biasing ckt.

a.c. signal $\Rightarrow i_c$ flows.

$$i_C = I_C + i_c$$

$I_C = \beta I_B$ Zero signal collector current

$i_C = \beta i_b$ Collector current due to signal.

iii] Emitter Cnt

No Signal = I_E flows $\rightarrow$ biasing ckt.

Signal applied = i_e

$$\therefore \cancel{I_E} \quad I_E = I_E + i_e$$

$\therefore$ wkt

$$I_E \approx I_C$$

$$i_e \approx i_c$$

$\therefore$ Base ckt is

Very very
small.

Types of Analysing.

1) D.C. Analysis

2) A.C. Analysis.

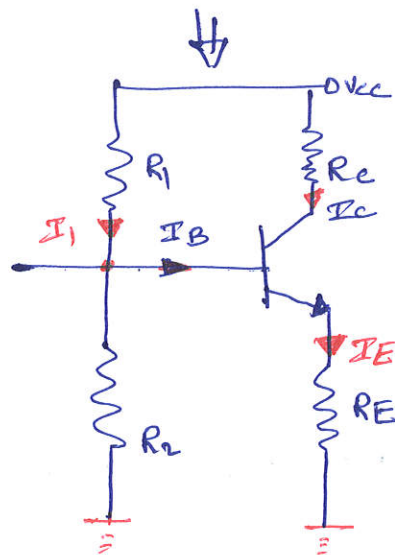
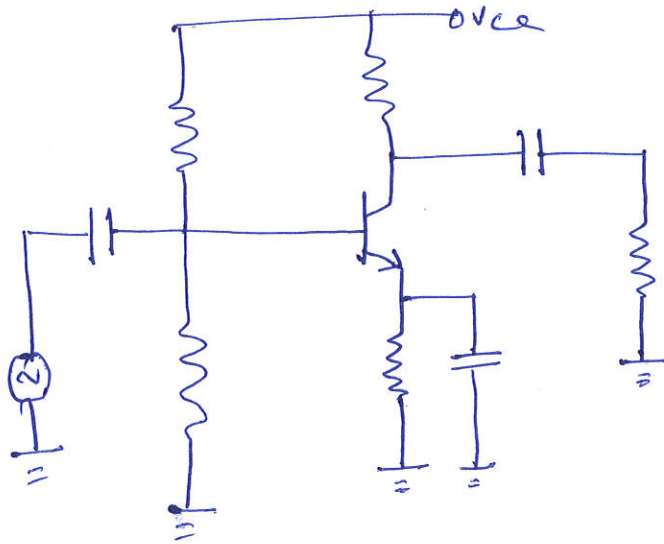
D.C. Equivalent Circuits.

$\rightarrow$ In the d.c. equivalent circuit of a transistor amplifier,

$\rightarrow$ As direct current cannot flow through a capacitor.

$\rightarrow$ all the capacitors look like open circuit in the d.c. equivalent circuit.

- * Reduces all a.c. sources to zero.
- * open all the capacitors.
- * calculate all the d.c. operating values.

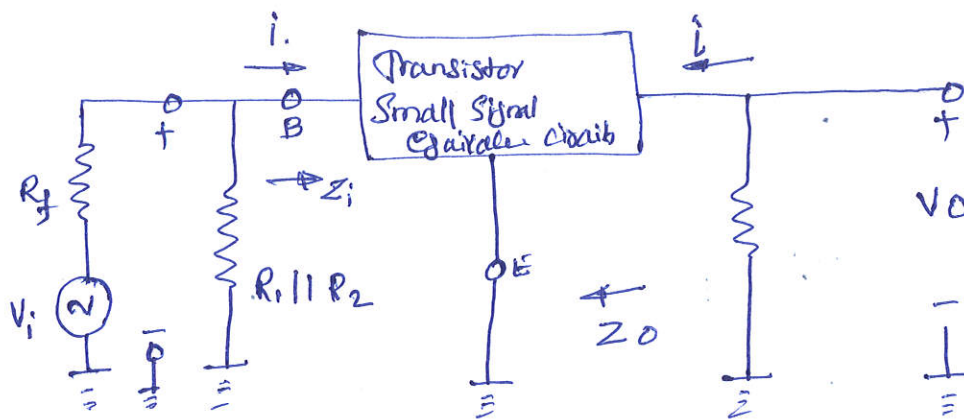


The A.c. Analysis.

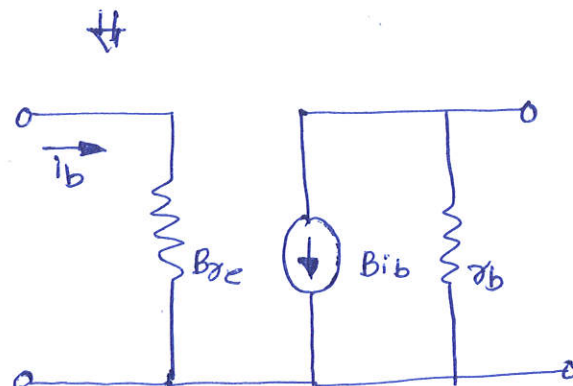
* only a.c. conditions are to be considered.

In order to draw the a.c. equivalent circuit the following two steps are applied.

- Reduce all d.c. sources to zero.
- Short all the capacitors.
- Calculate all necessary ac values.



Input Impedance. Z_i .



Base current is input current

I_c is the output current

$$I_c = \beta I_b$$

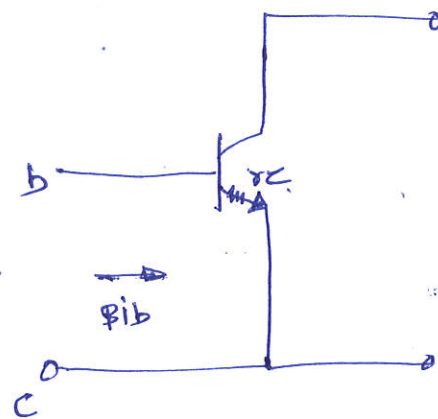
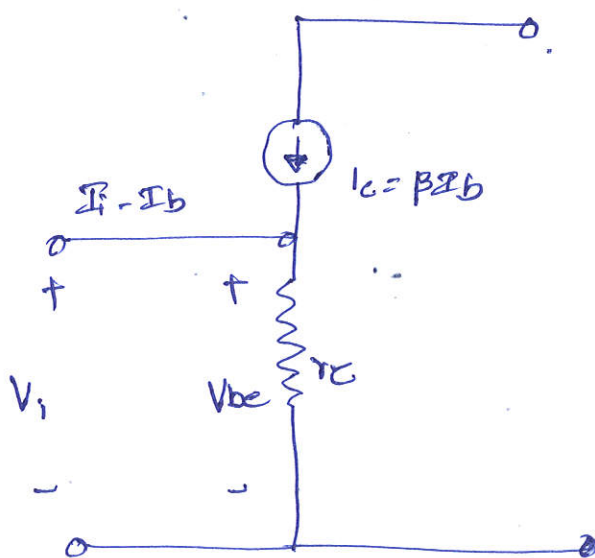
$$I_e = I_c + I_b$$

$$= \beta I_b + I_b$$

$$I_e = (\beta + 1) I_b$$

Since in AC, β is much greater than 1

$$\therefore I_e = \beta I_b$$



$$Z_i = \frac{V_i}{I_i} = \frac{V_{be}}{I_b}$$

The Voltage $V_{be} \rightarrow$ Across EBJ $\rightarrow$ Diode Resistance r_e

$$V_i = V_{be} = I_e r_e \approx \beta I_b r_e$$

$$Z_i = \frac{V_{be}}{I_b} = \frac{\beta I_b r_e}{I_b}$$

$$\boxed{Z_i = \beta r_e} \approx Z_i = r_b \parallel \beta r_e$$

Output Impedance

$$Z_o = R_c \parallel r_o$$

$$R_c \parallel r_o \approx R_c$$

$$\boxed{Z_o = R_c}$$

Voltage gain (A_v)

$$V_o = -I_o [R_c \parallel r_o] \quad \text{and} \quad V_i = I_i Z_i$$

$$= -[\beta I_b] [R_c \parallel r_o]$$

$$\boxed{V_i = I_b \beta r_e}$$

$$A_v = \frac{V_o}{V_i} \approx \frac{-[\beta I_b] [R_c \parallel r_o]}{I_b \beta r_e}$$

-ve sign

Indicates 180° phase shift

$$= - \frac{R_c || r_o}{r_e}$$

$$A_v = - \frac{R_c}{r_e}$$

r_o is very less or open.

Current gain (A_i)

$$A_i = \frac{I_o}{I_i} = \frac{I_c}{I_b} = \frac{\beta I_b}{I_b} = \beta$$

$$A_i \approx \beta$$

$$\text{or } A_i = \frac{I_o}{I_i} = \frac{V_o / R_c}{V_i / Z_i} = \left[\frac{V_o}{V_i} \right] \left[\frac{Z_i}{R_c} \right]$$

$$A_i = A_v \frac{\beta r_e}{R_c}$$

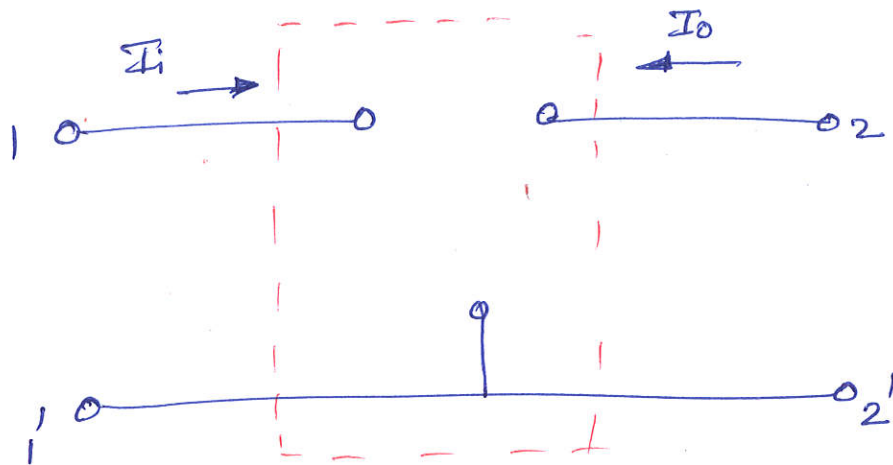
power gain.

$$A_p = \frac{P_o}{P_i}$$

$$= \frac{V_o I_o}{V_i I_i}$$

$$A_p = A_v \times A_i$$

hybrid equivalent circuit ac Analysis.



$$V_i = h_{11} I_i + h_{12} V_o$$

$$I_o = h_{21} I_i + h_{22} V_o$$

The four variables are called h-parameters.

→ hybrid

$$h_{11} = \frac{V_i}{I_i} \bigg|_{V_o=0}$$

$$h_{12} = \frac{V_i}{V_o} \bigg|_{I_i=0}$$

$$h_{11} = h_i$$

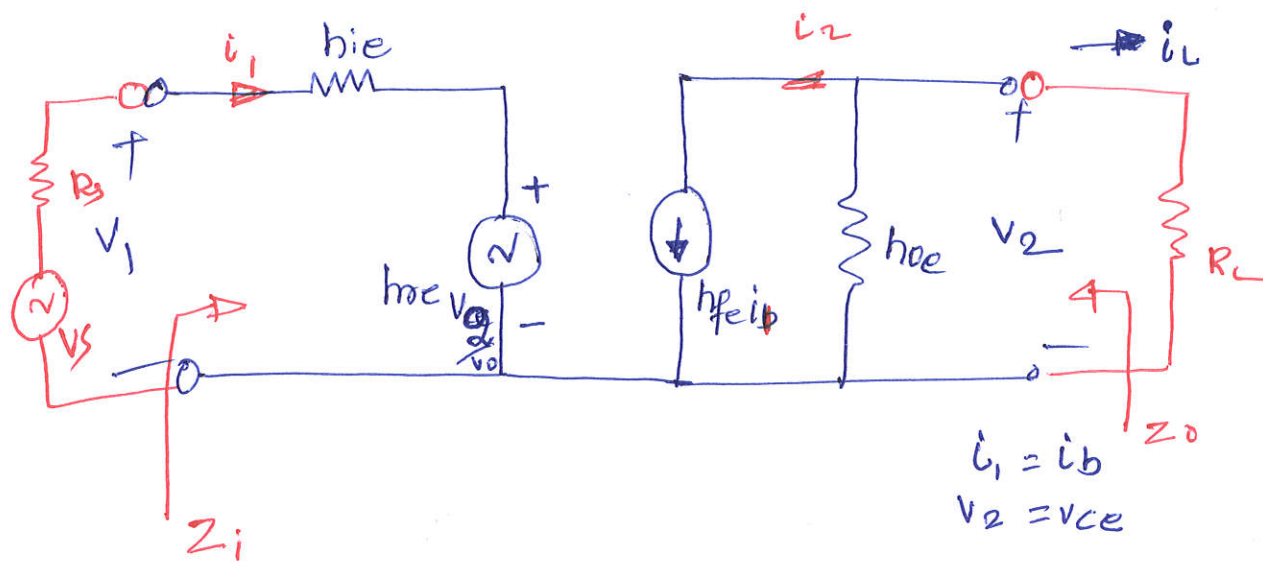
$$h_{12} = h_r$$

$$h_{21} = h_f$$

$$h_{22} = h_o$$

$$h_{21} = \frac{I_o}{I_i} \bigg|_{V_o=0}$$

$$h_{22} = \frac{I_o}{V_o} \bigg|_{I_i=0}$$



$$\begin{aligned} i_1 &= i_b \\ V_2 &= V_{ce} \\ i_2 &= i_c \\ V_2 &= V_{be} \end{aligned}$$

* current gain (A_i) = $\frac{o/p\ i}{i/p\ i} = \frac{i_L}{i_1} = \frac{-i_2}{i_1}$

$$V_2 = i_L R_L$$

$$V_2 = -i_2 R_L$$

$$i_2 = h_{fe} i_1 + h_{oe} (-i_2 R_L)$$

$$i_2 + h_{oe} i_2 R_L = h_{fe} i_1$$

$$i_2 (1 + h_{oe} R_L) = h_{fe} i_1$$

$$i_2 = \frac{h_{fe} i_1}{1 + h_{oe} R_L} \quad \alpha_{by} = -1/i_1$$

$$= \frac{i_2}{i_1} = \frac{-h f}{1 + h o R_L}$$

Q/

$$A_i = \frac{-h f}{1 + h o R_L}$$

Voltage gain, A_v

$$A_v = \frac{O/P_V}{I/P_V} = \frac{V_2}{V_1}$$

$$V_2 = -i_2 R_L$$

$$= \frac{-i_2 R_L}{V_1}$$

$$\therefore A_i = \frac{-i_2}{i_1}$$

$$-i_2 = i_1 A_i$$

$$\Rightarrow \frac{i_1 A_i R_L}{V_1}$$

o by both side i_1

$$= \frac{i_1 A_i R_L}{\cancel{i_1} \frac{V_1}{i_1}}$$

$$\Rightarrow \frac{A_i R_L}{Z_i} \quad \frac{V_1}{i_1} = Z_i$$

WKT

$$A_i = \frac{-h f}{1 + h o R_L}$$

$$Z_i = h_i - \frac{h_r h_f}{1/R_L + h_o}$$

$$= \frac{-h_f R_L}{h_i + \underbrace{(h_i h_o - h_r h_f)}_{\Delta h} R_L}$$

$$A_v = \frac{-h_f R_L}{h_i + \Delta h R_L}$$

power gain (A_p)

$$A_p = A_v \times A_i$$

$$A_p = \left(\frac{-h_f R_L}{h_i + \Delta h R_L} \right) \times \left(\frac{-h_f}{1 + h_o R_L} \right)$$

$$A_p = \frac{h_f^2 R_L}{(h_i + \Delta h R_L)(1 + h_o R_L)}$$

Input Impedance.

from ohm law.

$$V_i = I_i \times Z_i$$

$$Z_i = \frac{V_i}{I_i}$$

from eqn $V_1 = h_i i_1 + h_r V_2$

$$\therefore V_2 = -i_2 R_L$$

$$V_1 = h_i i_1 + h_r (-i_2 R_L)$$

$$V_1 = h_i i_1 + h_r V_2 \quad \text{--- (3)}$$

$$i_2 = h_f i_1 + h_o V_2 \quad \text{--- (4)}$$

$\div$ both side by i_1

$$\frac{V_1}{i_1} = h_i - \frac{h_r i_2 R_L}{i_1}$$

$$\frac{V_1}{i_1} = h_i + h_r A_i R_L$$

$$\left[A_i = \frac{-i_2}{i_1} \right] = \frac{-h_f}{1 + h_o R_L}$$

~~diff.~~

$$Z_i = h_i + h_r \left[\frac{-h_f}{1 + h_o R_L} \right]$$

$$Z_i = h_i - \frac{h_r h_f}{\frac{1}{R_L} + h_o}$$

Output Impedance.

$$R_L = \infty \rightarrow \text{①}$$

$$V_S = 0 \rightarrow \text{②}$$

* we need to sc V_S

* we need to as output terminal

$$Z_o = \frac{v_2}{i_2}$$

WKT

$$i_2 = h_f i_1 + h_o v_2$$

$$Z_o = \frac{v_2}{h_f i_1 + h_o v_2} \rightarrow \textcircled{1}$$

Apply KVL in input side

$$-i_1 R_s - i_1 h_i - h_r v_2 = 0$$

$$i_1 (R_s + h_i) + h_r v_2 = 0$$

$$i_1 = \frac{-h_r v_2}{R_s + h_i} \rightarrow \textcircled{2}$$

$$Z_o = \frac{v_2}{h_f \left[\frac{-h_r v_2}{R_s + h_i} \right] + h_o v_2}$$

$$Z_o = \frac{R_s + h_i}{[h_o h_i - h_f h_r] + h_o R_s}$$

$$Z_o = \frac{R_s + h_i}{\Delta h + h_o R_s}$$